Effect of Effective Refractive Index of Grating in FBG Splitter

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Abstract- The Fiber Bragg Gratings have been used extensively in the communication industry. Fiber Bragg grating is written directly into the core of the optical fiber and it is quite an attractive technique for wavelength splitter since it provides high reflectivity at a certain wavelength, with negligible transmission losses for others, providing a wavelength-channel selection with low crosstalk between adjacent channels. In this paper we propose a Fiber Bragg Grating base splitter with alteration of effective refractive index of grating for Ethernet passive optical network. With the increase in the effective refractive index the reflectivity of grating is increased. We analysed the effect of effective refractive index on reflectivity of grating. In our work the Bragg wavelength has been fixed at 1550 nm, length of the grating as 10mm and with effective refractive index as 4.0 it has been found that the reflectivity of the grating or the effectiveness of the grating in extracting the wavelength is 92-93%.

Index Terms-Fiber Bragg Grating; Reflectivity; Grating length; Effective refractive index of Grating.

1. INTRODUCTION

An optical fiber is an optical waveguide based on the principle of total internal reflection. In general, a proper description of the characteristics of an optical fiber is derived by solving the Maxwell’s equations. However, in order to get a general overview of the function of an optical fiber, it is suffice to consider the approximations of geometrical optics. In geometrical optics, Snell’s law dictates that light passing through an interface between two different materials refracts according to the relation:

$$\eta_1 \sin \theta_1 = \eta_2 \sin \theta_2 \quad (1)$$
Where $\eta_1$ and $\eta_2$ are the refractive indices of the two materials and $\theta_i$ and $\theta_t$ are the incidence and transmission angles respectively. If $\eta_1 > \eta_2$, then $\theta_t > \theta_i$, that is, if the first material has a higher refractive index than the second material, the transmission angle will be larger than the incidence angle. If the incidence angle is as large as the transmission angle would be, no light can be transmitted and instead all light will be reflected. This angle is called the critical angle ($\theta_c$).

$$\theta_c = \sin^{-1} \frac{\eta_2}{\eta_1}$$  \hspace{1cm} (2)

A standard telecom optical fiber usually has a core diameter of approximately 10 $\mu$m and a cladding with an external diameter of approximately 125 $\mu$m and can be manufactured to be several kilometres long.

In today’s era internet is growing day by day and the capacity requirement is increasing rapidly. This rapid increase in the requirement of capacity can be met by optical fiber communication. Fiber Bragg Grating (FBG) plays an important role in optical fiber communication. The FBG was initially demonstrated by Ken Hill in 1978. These gratings were fabricated using a visible laser, propagating along the fiber core. FBG are created by ‘inscribing’ or ‘writing’ systematic variation of refractive index into the core of a special type of optical fiber using an intense ultraviolet (UV) source such as a UV laser. Two main processes used are interference and masking. The methods used for creating FBG depend on the type of grating to be manufactured. A special germanium-doped silica fiber is used for the manufacturing of FBGs. In germanium-doped fiber the refractive index of the core changes with exposure to UV light and refractive index varies with variation in the amount of the intensity and duration of the exposure.

- **Interference**: This method is specifically used for uniform gratings. UV laser is split into two beams which interfere with each other creating a periodic intensity distribution along the interference pattern. The refractive index of the photosensitive fiber changes according to the intensity of light that is exposed on it.

- **Photo-mask**: The Photo-mask is placed between the UV light source and the photosensitive fiber. The shadow of the photo-mask then determines the grating structure based on the transmitted intensity of light striking the fiber. Photo-masks are specifically used in the manufacture of chirped FBGs, which cannot be manufactured using an interference pattern.

- **Point-by-point**: A single UV laser beam may also be used to 'write' the grating into the fiber point-by-point. In this technique the laser has a narrow beam that is equal to the grating period.

### 1.1. Fibre Bragg Grating (FBG)

FBGs are attractive as optical filters owing to their low insertion loss, compactness and cost efficiency [1]. These are formed by periodic variations of the refractive index in the core of an optical fiber. These periodic variations allow a FBG to pass the majority of light propagating through a fiber while reflecting back a narrow band of the incident light with a particular peak wavelength called the Bragg wavelength [2].

![Fig.1. Principle of operation of a Fiber Bragg Grating.](image)

FBG consists of a periodic modulation of the refractive index in the core of a single-mode optical fiber as presented in Fig. 1. In uniform fiber gratings, the phase fronts are perpendicular to the fiber longitudinal axis and with the grating planes having constant period are considered the fundamental building blocks for most Bragg grating structures. Light guided along the core of an optical fiber is scattered by each grating plane; if the Bragg condition is
not satisfied, the reflected light from each of the subsequent planes becomes progressively out of phase and will eventually cancel out. Where the Bragg condition is satisfied, the contributions of reflected light from each grating plane add constructively in the backward direction to form a back-reflected peak with a center wavelength defined by the grating parameters. \( \eta_{\text{eff}} \) & \( p \) are the effective indices of refraction of the fiber and the pitch of the grating in the fiber respectively. Depending on the intensity and pitch of the grating, numerous types of functions have been proposed. The reflected wavelength is given by the Eq. (3):

\[
\lambda_B = 2\eta_{\text{eff}} p
\]  

(3)

The Bragg relationship in its differential form is given by Eq.(4):

\[
\Delta \lambda_B = \lambda_B \left( \frac{\Delta n}{n_0} + \frac{\Delta p}{p} \right)
\]  

(4)

These equations state that any measurable quantity applied to the grating that causes a refractive index change or period change, induces a deviation in the resonant wavelength.

A uniform grating can be represented by a sinusoidal modulation of the refractive index of the fiber core given by Eq.(5):

\[
n(z) = n_{\text{core}} + \delta n \left[ 1 + \cos \left( \frac{2\pi z}{p} + \phi z \right) \right]
\]  

(5)

1.2. Sensors

FBG sensors are based on the fact that the Bragg wavelength changes with change in the pitch of the grating and the change in the refractive index. Thus, any physical parameter (like temperature, strain, stress) which causes changes in the above mentioned parameters can be sensed using a FBG, by measuring the shift in the Bragg wavelength or the change in reflection coefficient of a particular wavelength [3].

Optical fibre sensors and their systems have the following advantages [4, 5, and 6]:

- The low transmission loss of optical fibre enables remote sensing over tens of kilometres.
- Real time monitoring is achieved by connecting the sensor heads directly to the measuring equipment using optical fibre.
- Easy to install due to small size.
- Can be multiplexed.
- High sensitivity.
- Integrated telemetry: fibre itself is a data link.
- Possibility of remote, multiplexed operation.

2. LITERATURE SURVEY

Ming Li; et al. [1], demonstrated a novel multi-channel notch filter with a multiplicable channel count by utilizing both multiple-phase-shift and sampling techniques. Reema Sharma; et al [3], concluded that change in pitch of grating changes the reflection coefficient of interrogating wavelength. By observing this change, the strain in fibre can be calculated and corresponding measurements can be made. They also inferred that increase in the pitch will change the reflectivity of the interrogating wavelength. As per their results at particular value of pitch the maximum reflective power for interrogating wavelength is 94.6%. Bashir Ahmed Tahir; et al.[7], investigated on tracking of Bragg wavelength shifts caused by the changes in load. The FBG system is more sensitive to smaller sensor lengths and less sensitive to larger sensor lengths. Ing.Radek HELAN; et al [8], investigated that spectral properties of grating depends upon the grating length, refractive index changes and \( \delta n \). They concluded that longer grating with low \( \delta n \) value causes more narrow bandwidth and shorter grating with high \( \delta n \) value causes more wide bandwidth. Gemzický; et al [9], simulated the reflectance’s of FBGs with different grating lengths and different modulations of
the refractive index. Their results proved that the increase of the grating length causes the decrease in bandwidth and the increase of the reflectance at the Bragg wavelength. This could be used for narrow-band wavelength selective filtering. Mohammad Syuhaimi; *et al.* [10], worked on the effects of refractive index of cladding to Bragg wavelength and reflection in waveguide Bragg grating filter. The increase of cladding index value in certain duration does not affect the reflected wavelength. The range was bigger when the values were far from the core index and the size becomes smaller when the cladding index values achieve the core index value. Bashir Ahmad Tahir; *et al.* [11], described a FBG sensing system for strain measurements. They investigated the two parameters reflectivity and Bragg wavelength shift. They observed a negligible change in reflectivity by changing in index modulation from 0.0001 and 0.0008. The average value of reflectivity was found to be 95%. The reflectivity almost remains constant, even though by varying the index modulation. Tran Thi Tam; *et al.* [12], investigated the temperature responses of the FBGs. It was found that these responses ranged from 10.6 pm/°C to 12.0 pm/°C. The temperature sensitivity of the FBGs was 0.2°C. Although the temperature response is nonlinear over the temperature range 20°C to 180°C, in practical systems the temperature response of the sensor may be assumed to be linear within the temperature range 20°C to 80°C.

3. ANLYTICAL MODEL

In this paper, a wavelength splitter has been proposed for single mode fiber using FBG. The Analytical model has been proposed for the reflectivity of grating which is given by Eq.(6).

**Assumptions:**

- Length of Grating, \( l = 10 \text{mm} \)
- Index difference between core and cladding, \( \Delta = 0.0036 \)
- Bragg Wavelength, \( \lambda_g = 1550.08 \text{ nm} \)
- Radius of core, \( a = 4.5 \mu\text{m} \)
- Index amplitude of grating, \( \Delta n = 1 \times 10^{-4} \)

**Reflectivity:**

\[
R = \frac{\sinh^2 \left[ \sqrt{c^2 - \delta^2} \right]}{\cosh^2 \left[ \sqrt{c^2 - \delta^2} \right] - \left( \frac{c}{p} \right)^2}
\]

(6)

\[
\delta = \beta - \left( \frac{c}{p} \right)
\]

(7)

\[
\beta = \frac{2 \eta n_{\text{eff}}}{\lambda_g}
\]

(8)

\[
p = \frac{\lambda_g}{2 \eta n_{\text{eff}}}
\]

(9)

\[
c = \frac{\eta}{\lambda_g}
\]

(10)

\[
\eta = \Delta n \times P_c
\]

(11)

Where

- \( \delta \) is detuning factor
- \( \beta \) is propagation constant
- \( p \) is pitch of the grating
- \( c \) is coupling coefficient
- \( \eta \) is overlap integral between forward and reverse propagating mode.
Here ‘\( P_c \)’ is fractional power of core and is given by \( P_c = \left[ 1 - \frac{1}{v^2} \right] \), where \( v \) is the normalized frequency.

4. SIMULATION, RESULTS & DISCUSSION

The simulation is carried out on simulation Software MATLAB 7.2 of Math-works. The simulation model thus constructed has improved the reflectivity of the fiber grating with variation of some of the design parameters. In this paper effective refractive index of grating has been varied to achieve the maximum reflectivity for the wavelengths for Ethernet Passive Optical Networks (EPON).

In Fig. 4. Effectiveness of the grating was calculated as 8.49% for 0.7 effective refractive index. It was increased to 36.78% and 56.84% when the effective refractive index was increased to 0.8 and 0.9.

In Fig. 5 the reflectivity of the grating was calculated to be 68.49% for the effective refractive index of 1.0, which was increased to 79.82%, 84.79 %, when the effective refractive index was increased to 1.2 and 1.4 respectively.

In Fig. 6 the reflectivity of the grating or the effectiveness of the grating was calculated as 87.39% for 1.6 effective refractive index. It was increased to 89.91% when the effective refractive was increased to 2.0. Further it was increased to 92.48% with 4.0 effective refractive index. Now the changes in value of reflectivity are negligible with the variation of effective refractive index so we stopped simulation here.

![Reflection varying with Effective refractive index of Grating](image_url)
Fig 5: Reflection varying with effective refractive index of grating $n_{eff} = 1.0, 1.2$ and $1.4$

Fig 6: Reflection varying with effective refractive index of grating $n_{eff} = 1.6, 2.0$ and $4.0$
5. CONCLUSION

We have analysed the effect of effective refractive index of grating on response of reflectivity of Fibre Bragg grating having centre wavelength 1550nm. For effective refractive index of 0.7 to 2.0, reflectivity is not sufficient to extract the wavelength effectively. From the simulation results it can be concluded that reflectivity was sufficient to extract the wavelength effectively with value ‘4’ of effective refractive index of grating when length of grating was 10mm. If we further increased its value the change in reflectivity was negligible. So with the increase in the effective refractive index the reflectivity of grating increases to some extent thereafter changes in values of reflectivity are very small.

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